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Abstract: Let $f : [a, b] \rightarrow \mathbb{R}$ be a continuous function such that the n -th order symmetric Laplace derivative $SLD^n f$ exists in (a, b) . It is proved that if $SLD^n f, SLD^{n-2} f, SLD^{n-4} f, \dots$ are Darboux and Baire*1 in (a, b) and if the upper symmetric Laplace derivative $\overline{SLD}^{n+2} f$ is non-negative in (a, b) , then the ordinary n -th order derivative $f^{(n)}$ exists and is convex in (a, b) .

Johnsy S. Prasad and A. R. Rajan

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Xueqin Wang, Chunlin Lei and Chunfang Chen

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P. N. Natarajan

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Kailash Lachhwani

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R. Anantharaman

BANACH SPACES IN CLASSICAL HARMONIC ANALYSIS 217-241

Abstract: In this paper we consider some connections between Banach spaces and classical Harmonic Analysis. We let $T = R/2\pi Z$:

(i) Majority of elements (in sense of Baire's category) in the Banach Space c_0 (or l^∞) cannot be (sequence of) Fourier coefficients of any function in $L^1(T)$ or measure (respectively in $rea(T)$, the Banach space of regular real valued measures on Borel sets of T).

Further a majority of functions (or measures) in both spaces have the property that the sequence of their Fourier coefficients do not belong to l^p for any $p \geq 1$.

(ii) In connection with the Hausdorff-Young theorem, a similar statement holds for the spaces l^q and the space L^p for $1 < p < 2 < q$, where p and q are conjugates.

(iii) Lacunary series in $C(T)$.

(iv) A theorem that a certain (closed) subspace C_Λ of $C(T)$ has Cotype 2 iff Λ is a Sidon set.

(v) We mention the intriguing classical fact related to a result of Marcel Riesz, i.e. for $1 < p < \infty$ the trigonometric system is a Schauder basis in L^p . (It is an unconditional one only if $p = 2$).
